

Machine Learning (CS 181): Style Guide

Basic Notation

$\mathbf{A} \in \mathbb{R}^{m \times n}$	matrices are bold caps
$\mathbf{a} \in \mathbb{R}^{m(\times 1)}$	vectors are bold lower, always column
\mathbf{a}^\top	transpose
$a \in \mathbb{R}$	scalars are lower case, non bold
\mathcal{A}	sets are script case
$\{\mathbf{a}_i\}_1^n$	a sequence of $\mathbf{a}_1 \dots \mathbf{a}_n$

- ▶ We distinguish between \mathbf{a}_i and b_i . The first is the *i'th* vector of a sequence, the second is the *i'th* scalar in \mathbf{b} .

Supervised Learning

$\mathbf{X} \in \mathbb{R}^{n \times m}$ n training instances with m features

$X_{i,j}$ the j 'th feature of example i

$\mathbf{y} \in \mathbb{R}^n$ the n target instances (regression)

$\mathbf{y} \in \{-1, 1\}^n$ the n target instances (classification)

- ▶ When describing data as a sequence we use

$$D = (\mathbf{x}_1, y_1) \dots (\mathbf{x}_n, y_n) = \{(\mathbf{x}_i, y_i)\}_1^n$$

Models

$\mathbf{w} \in \mathbb{R}^m$	linear-model parameters
$f(x; \mathbf{w})$	model parameterized by \mathbf{w}
\hat{y}	model prediction (to be distinguished from target y)
$\phi : \mathbb{R}^m \mapsto \mathbb{R}^d$	basis function (if used changes \mathbf{w} dim)

Optimization

- ▶ $\mathcal{L}(\mathbf{w})$; loss function
- ▶ $\mathbf{w}^* = \arg \min_{\mathbf{w}} \mathcal{L}(\mathbf{w})$; training minimization
- ▶ $\mathcal{L}(\mathbf{w}) = - \sum_{i=1}^n \ln p(y_i | \mathbf{x}_i; \mathbf{w})$; negative log-likelihood
- ▶ $\min_x \mathbf{x}$ s.t. $\mathbf{Ax} = \mathbf{b}$; constrained

Probabilistic Notation

- ▶ $p(y | x)$; discrete distribution $p(Y = y | X = x)$ (RVs implied)
- ▶ $p(y | x) \propto p(x | y)p(y)$; proportional to notation
- ▶ $\mathcal{N}(x | \boldsymbol{\mu}, \boldsymbol{\Sigma})$; multivariate normal (prefer exp to e)

$$\mathcal{N}(x | \boldsymbol{\mu}, \boldsymbol{\Sigma}) = \frac{1}{\sqrt{|2\pi\boldsymbol{\Sigma}|}} \exp\left(-\frac{1}{2}(\mathbf{x} - \boldsymbol{\mu})^\top \boldsymbol{\Sigma}^{-1}(\mathbf{x} - \boldsymbol{\mu})\right)$$

- ▶ α, β, γ ; scalar hyperparameters (explicitly conditioned $p(w|\alpha)$)
- ▶ $\boldsymbol{\alpha}, \boldsymbol{\beta}, \boldsymbol{\gamma}$; vector hyperparameters